

Theory of Fuzzy Sets and the Social Sciences

Mr. Mohan Bikram Malla, Er. Saleena Dahal

Mid-West University, Graduate School of Engineering, Birendranagar- Surkhet

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ABSTRACT

It is obvious that humans are typically associated with fuzziness in real-world problems. However, social scientists have been using fuzzy set theory to solve complicated problems far later than they should have. Fuzzy well understood that the nature of the mind is inherently vague and complex. However, our social environment is also somewhat unclear. In a variety of social sciences, fuzzy sets offer a mathematical modeling method for expressing ambiguity. In general, this kind of problem has a lot of parameters. We ought to enhance our data analysis and derive more precise findings by transitioning from deterministic mathematical modeling to probabilistic modeling, and then to fuzzy modeling.

Keywords: Social sciences, mathematical modeling, and fuzzy set theory

FUZZY LOGIC AND MATHEMATICAL APPROACHES FOR MODELING SYSTEMS

Mathematics is fundamentally an abstract discipline. The historical development of mathematics illustrates that it is ingrained in our civilization. No one is able to consider themselves truly well-educated until they understand fundamental mathematics ideas. It is a sophisticated language and an essential instrument for demonstrating the interrelations among many scientific disciplines. All disciplines of mathematics can assist us tackle the challenges We see various mathematical disciplines in science and engineering. Subjects such as symbolic logic, relations, limits and continuity in topology, function theory, analytic geometry, abstract algebra, calculus, differential geometry, differential equations, and linear algebra are utilized to address intricate challenges in these fields.(Russell, 2020).

If we understand the importance of fuzzy logic, we may predict that it will be used in a wide range of fields. Unfortunately, a few scholars in the disciplines of humanities and social sciences are familiar with fuzzy set theory. Some scholars in the fields of engineering, especially industrial engineering, and mathematics are exploring the use of fuzzy set theory in areas beyond engineering.

The theory of fuzzy sets, being an established theoretical framework, evolves throughout time, becoming more complicated, detailed, expanded, and producing new ideas and concepts. It incorporates traditional mathematical concepts such as algebraic processes, graph analysis, topology, and related topics. Fuzzy logic serves as an effective modeling tool capable of handling diverse uncertainties and addressing real-world challenges. Due to its broad applicability, fuzzy set theory can be readily used across a wide range of scenarios (Özok, 2021).

Fuzzy set operations in applied mathematics are very popular among mathematicians. Examples of this type include clustering techniques, control strategies, and mathematical programming methods. (Kahraman, 2006) . Fuzzy approaches are also used in transportation, logistics, inventory control, and other areas. Other applications of fuzzy logic include Fuzzy expert systems and fuzzy control methods.

Lastly, fuzzy set theory's use in the social sciences is probably going to spread to other domains. Although it may appear that the social sciences and humanities are somewhat apart from mathematics, fuzzy set theory makes an effort to gradually integrate itself into applicability of problems in the real world.

CREATION OF APPLICATIONS FOR FUZZY SETS

The challenge is that a lot of significant social science concepts are not able to be classified as either member or non-members of the set. Core ideas in the social sciences and humanities are best grasped as graded sets. Examples that can be viewed as graded sets include politics, economics, democracy, and more. Many scientists recognize the drawbacks of relying on simple dichotomies at the theoretical level. Sadly, this understanding has not been transferred into the use of completely diverse and complicated approaches.

According to fuzzy set theory, social scientists can view all phenomena can be viewed as sets with unclear boundaries for membership and non-membership. Additionally, it allows us to finalize the membership score within the $[0, 1]$ range. We can think of the fuzzy set as a continuous variable in this way. Regarding the membership score, the maximum ambiguity point is 0.5 (Smithson, 2006) .

We can perform set-based operations like union, intersection subset, multiplication, requirement, and sufficiency under vagueness thanks to fuzzy set theory. The social sciences allow for the explicit formulation of verbal theory in terms of set theory. Once more, set-theoretic relations allow us to characterize ambiguity and diversity. In the social sciences and humanities, fuzzy sets enable a more complex depiction of categorical notions.

It is also feasible to apply hybrid models in many study domains; by this, I refer to the integration of probabilistic, fuzzy, and deterministic models in a certain problem domain. Regrettably, one of the shortcomings of a large portion of research on fuzzy sets is membership assignments. Aside from the ambiguity of social science topics, another issue is the absence of clear definitions. Another challenge is determining how to quantify the idea in question.

IN ESSENCE

Fuzzy set theory offers extensive applications and numerous research areas. Key research areas include the following:

- Practical Mathematics
- Intelligent systems and machine learning algorithms
- Data Analytics and Large-Scale Data Processing
- Medical Diagnosis and Healthcare
- Control Systems and Automation
- Finance and Economics

In each case, we must demonstrate that fuzzy theoretic solutions get the best results. It must be compared to alternative approaches to the problem, if at all possible. The biggest challenge, in my opinion, is to comprehend only the fundamental ideas and philosophy of mathematics. Each issue must be treated in accordance with the principal parameters. The old notions are undervalued and replaced with bizarre inventions that have no place in science or engineering Should we neglect to comprehend the intricate relationships among mathematical notions.

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